Orbital Motion in Outer Solar System

J. Klačka ¹, M. Gajdošík ²

¹Astronomical Institute, Faculty of Mathematics and Physics, Comenius University Mlynská dolina, 842 48 Bratislava, Slovak Republic ²Ostredská 20, 821 02 Bratislava, Slovak Republic

Motion of a point mass in gravitational fields of the Sun and of the galactic disk is studied. Fundamental features of the motion are found by investigating the time-averaged differential equations for orbital evolution. Several types of possible orbits are mathematically exactly derived in a strictly analytical way. The relation $a^3 P^2 = f(e_0, i_0, \omega_0)$ between semimajor axis a and period P of the change of osculating orbital elements is found (the index 0 denotes initial values of the quantities).

Due to conservation of energy in potential fields a is a constant. Moreover, the component of angular momentum perpendicular to the galactic plane is conserved. Due to these facts the system of equations reduces to two equations for either (e, ω) , or (i, ω) (the length of the ascending node does not enter the equations for a, e, i, ω and is not solved here).